A Model of the Twin Ds: Optimal Default and Devaluation

by Na, Schmitt-Grohe, Uribe and Yue

Discussion by Anastasios Karantounias, Federal Reserve Bank of Atlanta December 12, 2014

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- Quantitative study of the joint default and devaluation/capital controls properties. Analyze also pegging.

Discussion plan

- Overview of the model.
- Some thoughts about the setup.

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• Some questions.

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- Production of non-tradeables with labor from a competitive firm.
- Labor markets do not clear due an ad hoc downward wage rigidity.
- Government: Taxes holdings of external debt, chooses exchange rate policy, provides transfers and decides each period to honor or not the private agent's liability.

• Utility of agent: $E_0 \sum_{t=0}^{\infty} \beta^t U(c_t), c_t = A(c_t^T, c_t^N)$

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- Debt holdings:

$$(1 - \tau_t^d)q_t^d = \beta E_t \frac{U'(c_{t+1})A_{1,t+1}}{U'(c_t)A_{1t}}$$

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• If unemployment $h_t < \bar{h} \Rightarrow$ wages do not adjust enough downwards, $W_t = \gamma W_{t-1}$. If $W_t > \gamma W_{t-1} \Rightarrow h_t = \bar{h}$.

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- Due to the nominal rigidity, real wage can be above the full-employment real wage, $F'(\bar{h})$.

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- Foreign lender: prices the default risk.

$$q_t = \frac{Prob_t(\text{repayment at } t+1)}{1+r^*}$$

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Competitive equilibrium

• Given policy $\{\tau_t^d, \epsilon_t, I_t\}_{t=0}^{\infty}$: a price system $\{p_t, w_t, q_t\}$ and an allocation $\{c_t^T, c_t^N, h_t, d_{t+1}\}$ such that everybody maximizes and markets clear.

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- Resource constraint

$$c_t^T = y_t^N - (1 - I_t)L(y_t^N) + I_t[q_t d_{t+1} - d_t]$$

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• Optimal policy: choose $\{\tau_t^d, \epsilon_t, I_t\}_{t=0}^{\infty}$ to maximize utility of the household subject to conditions of the CE.

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 - **1** Government issues public debt that it can default on.

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 - 2 Allocation c_t^T, d_{t+1} and default choices same as in Arellano, but accompanied with the proper choice of $\{\tau_t^d, \epsilon_t\}$.
- A model with centralized external borrowing delivers the same predictions as a model with the decentralized external borrowing, a government that can confiscate external payments as long as the government has free access to exchange rate policy and capital controls.

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• Optimal devaluation: Any ϵ_t such that

$$\epsilon_t \ge \gamma \frac{w_{t-1}^f}{w_t^f}$$

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- Focus on $\epsilon_t = \frac{w_{t-1}^t}{w_t^t} \Rightarrow$ keep the nominal wage constant.
- Choose capital controls as a *residual*:

$$1 - \tau_t^d = \beta (1 + r^*) \frac{E_t \frac{U_{T,t+1}}{U_{T,t}}}{Prob_t (\text{repayment})}$$

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- Same equivalence would hold but *different* capital controls.
- Is it possible to interpret the current setup as private agents borrowing from the government (at q_t^d) and government borrowing from abroad?

• Assume that $c_t^T \downarrow \Rightarrow$ demand for $c_t^N \downarrow \Rightarrow$ price p_t falls $\Rightarrow w_t/p_t \uparrow \Rightarrow$ demand for labor falls. To restore full employment need to reduce w_t by devaluing.

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• Devaluation+ Default.

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- Value of repayment

$$V^{r}(d, w_{-}, y) = \max_{c, h, d', w} U(A(c, F(h))) + \beta E_{y'|y} V(d', w, y')$$

subject to

$$c + d = y + q(d', w, y)d'$$
$$w = \frac{A_2(c, F(h))}{A_1(c, F(h))}F'(h)$$
$$w \ge \gamma w_-$$
$$h \le \bar{h}$$

• With optimal devaluation

$$u'(A)A_1(c, F(\bar{h}))[\underbrace{\frac{\partial q(d', y)}{\partial d'}d' + q(d', y)]}_{MR^{\text{optimal}}} = -\beta \frac{\partial}{\partial d'} E_{y'|y}V(d', y')$$

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- Additional marginal benefit of borrowing if $MR^{\text{optimal}} = MR^{\text{pegging}}$.

• Find quantitatively that less debt can be sustained in equilibrium with pegging.

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- Steepness of the price schedule/MR from debt issuance?
- Play around with the intertemporal and intratemporal substitutability in order to see how default/repayment regions change. For the current exercise marginal utility of tradeables does not depend on labor.

- Subsidize purchases of labor by firms. Finance firm-subsidy by lump-sum taxes on consumer.
- After-subsidy wage: $(1 \kappa)W$.
- Profits:

$$\Pi_t = P_t^N F(h_t) - (1 - \kappa_t) W_t h_t \Rightarrow F'(h_t) = (1 - \kappa_t) \frac{W_t}{P_t^N} = (1 - \kappa_t) \frac{w_t}{p_t}$$

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- Schmitt-Grohe and Uribe (2013) have also considered this firm subsidy.
- Would be interesting to see $\{\tau_t^d, \kappa_t\}$ induced by the optimal default allocation.